

Static Program Analysis Meets Test Case Generation

Lecture 3

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Textbook: Weakest Preconditions

Verification condition

- Logic formula reflecting the correctness of a program
- Typically checked by an automatic theorem prover
- Equivalent formulations can affect performance

Verification condition

- Logic formula reflecting the correctness of a program
- Typically checked by an automatic theorem prover
- Equivalent formulations can affect performance

A technique for computing verification conditions is
weakest preconditions

A simple language

$S, T ::= Id := Expr$

A simple language

$$S, T ::= Id := Expr$$
$$| \text{ **assert** } Expr$$

A simple language

$$\begin{aligned} S, T ::= & \text{Id} := \text{Expr} \\ & | \text{assert } \text{Expr} \\ & | \text{assume } \text{Expr} \end{aligned}$$

A simple language

$$\begin{aligned} S, T ::= & \text{Id} := \text{Expr} \\ & | \text{assert } \text{Expr} \\ & | \text{assume } \text{Expr} \\ & | S ; T \end{aligned}$$

A simple language

$$\begin{aligned} S, T ::= & \text{Id} := \text{Expr} \\ & | \text{assert } \text{Expr} \\ & | \text{assume } \text{Expr} \\ & | S ; T \\ & | S \square T \end{aligned}$$

Exercise

Is this simple language rich enough to encode if-statements?

if B **then** S **else** T **end**

$S, T ::= Id := Expr$

| **assert** $Expr$

| **assume** $Expr$

| $S ; T$

| $S \square T$

Exercise

Is this simple language rich enough to encode if-statements?

if B then S else T end

Yes!

(assume B ; S) \square (assume $\neg B$; T)

Weakest precondition

$$wp(S, Q)$$

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characterizes all pre-states from which

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$$wp(S, Q)$$

characterizes all pre-states from which
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does not go wrong and terminates

Weakest precondition

$$wp(S, Q)$$

characterizes all pre-states from which
every non-blocking execution of S
does not go wrong and terminates
in a state satisfying Q

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

Example:

$$wp(x := y, 0 < x) \equiv 0 < y$$

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

Exercise:

$$wp(x := x + 1, 0 < x) \equiv$$

Weakest precondition

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Exercise:

$$wp(x := x + 1, 0 < x) \equiv 0 < x + 1$$

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

Exercise:

$$wp(x := x + 1, 0 < x) \equiv 0 < x + 1$$

$$wp(x := x + 1, z - 2 < y) \equiv$$

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

Exercise:

$$wp(x := x + 1, 0 < x) \equiv 0 < x + 1$$

$$wp(x := x + 1, z - 2 < y) \equiv z - 2 < y$$

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

$$wp(\mathbf{assert} Expr, Q) \equiv Expr \wedge Q$$

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$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

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Exercise:

$$wp(\mathbf{assert} \mathbf{false}, Q) \equiv$$

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

$$wp(\mathbf{assert} Expr, Q) \equiv Expr \wedge Q$$

Exercise:

$$wp(\mathbf{assert} \mathbf{false}, Q) \equiv \mathit{false}$$

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

$$wp(\mathbf{assert} Expr, Q) \equiv Expr \wedge Q$$

$$wp(\mathbf{assume} Expr, Q) \equiv Expr \Rightarrow Q$$

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

$$wp(\mathbf{assert} Expr, Q) \equiv Expr \wedge Q$$

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$$wp(S ; T, Q) \equiv wp(S, wp(T, Q))$$

Weakest precondition

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

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$$wp(S ; T, Q) \equiv wp(S, wp(T, Q))$$

$$wp(S \square T, Q) \equiv wp(S, Q) \wedge wp(T, Q)$$

Exercise

What is the weakest precondition of the if-statement?

if B then S else T end

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

$$wp(\mathbf{assert} Expr, Q) \equiv Expr \wedge Q$$

$$wp(\mathbf{assume} Expr, Q) \equiv Expr \Rightarrow Q$$

$$wp(S ; T, Q) \equiv wp(S, wp(T, Q))$$

$$wp(S \square T, Q) \equiv wp(S, Q) \wedge wp(T, Q)$$

Exercise

What is the weakest precondition of the if-statement?

$$(\mathbf{assume} \ B ; S) \sqcup (\mathbf{assume} \ \neg B ; T)$$

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

$$wp(\mathbf{assert} \ Expr, Q) \equiv Expr \wedge Q$$

$$wp(\mathbf{assume} \ Expr, Q) \equiv Expr \Rightarrow Q$$

$$wp(S ; T, Q) \equiv wp(S, wp(T, Q))$$

$$wp(S \sqcup T, Q) \equiv wp(S, Q) \wedge wp(T, Q)$$

Exercise

What is the weakest precondition of the if-statement?

$(\text{assume } B ; S) \square (\text{assume } \neg B ; T)$

$$B \Rightarrow wp(S, Q) \wedge \neg B \Rightarrow wp(T, Q)$$

Verification condition

For a given program P , the verification condition is

$$wp(P, true)$$

Verification condition

For a given program P , the verification condition is

$$wp(P, true)$$

This condition is valid **if and only if** P is free of errors

Exercise

What is the weakest precondition of the program?

(assume B ; $x := 1$) \square **(assume $\neg B$; $x := -1$)**

Assume that Q is $x = 2$.

$$B \Rightarrow wp(S, Q) \wedge \neg B \Rightarrow wp(T, Q)$$

$$wp(x := Expr, Q) \equiv Q[x := Expr]$$

Exercise

What is the weakest precondition of the program?

(assume B ; $x := 1$) \square **(assume $\neg B$; $x := -1$)**

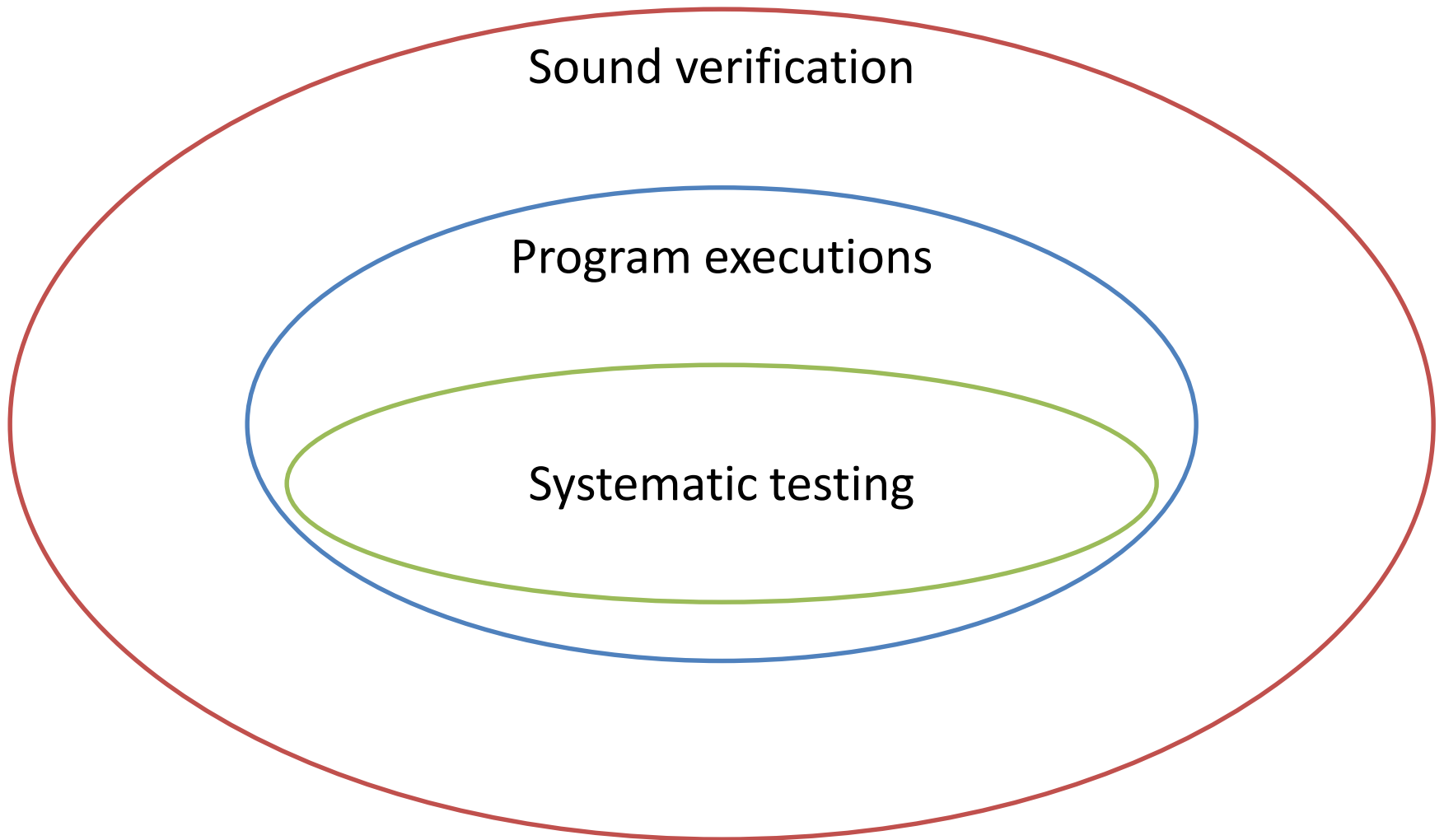
Assume that Q is $x = 2$.

false

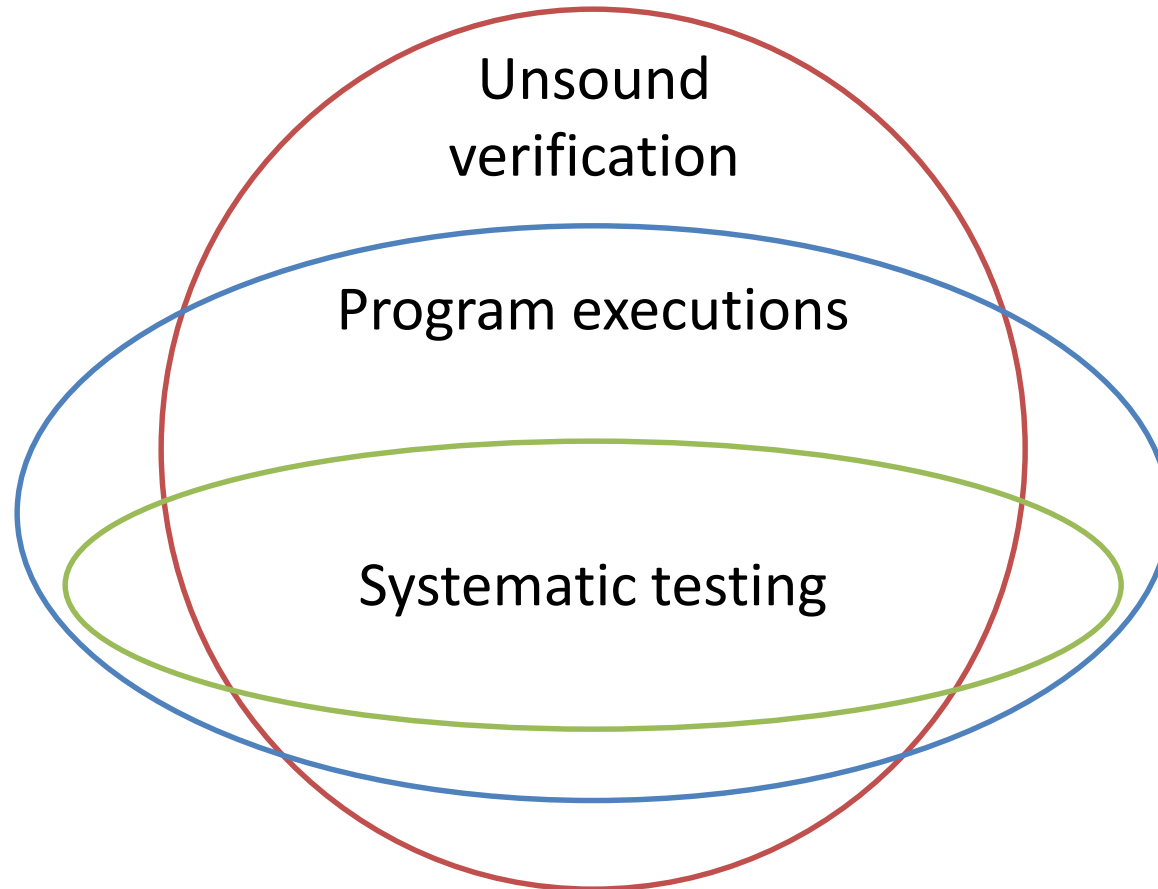
Fun:

Guiding Dynamic Symbolic Execution
toward Unverified Program Executions

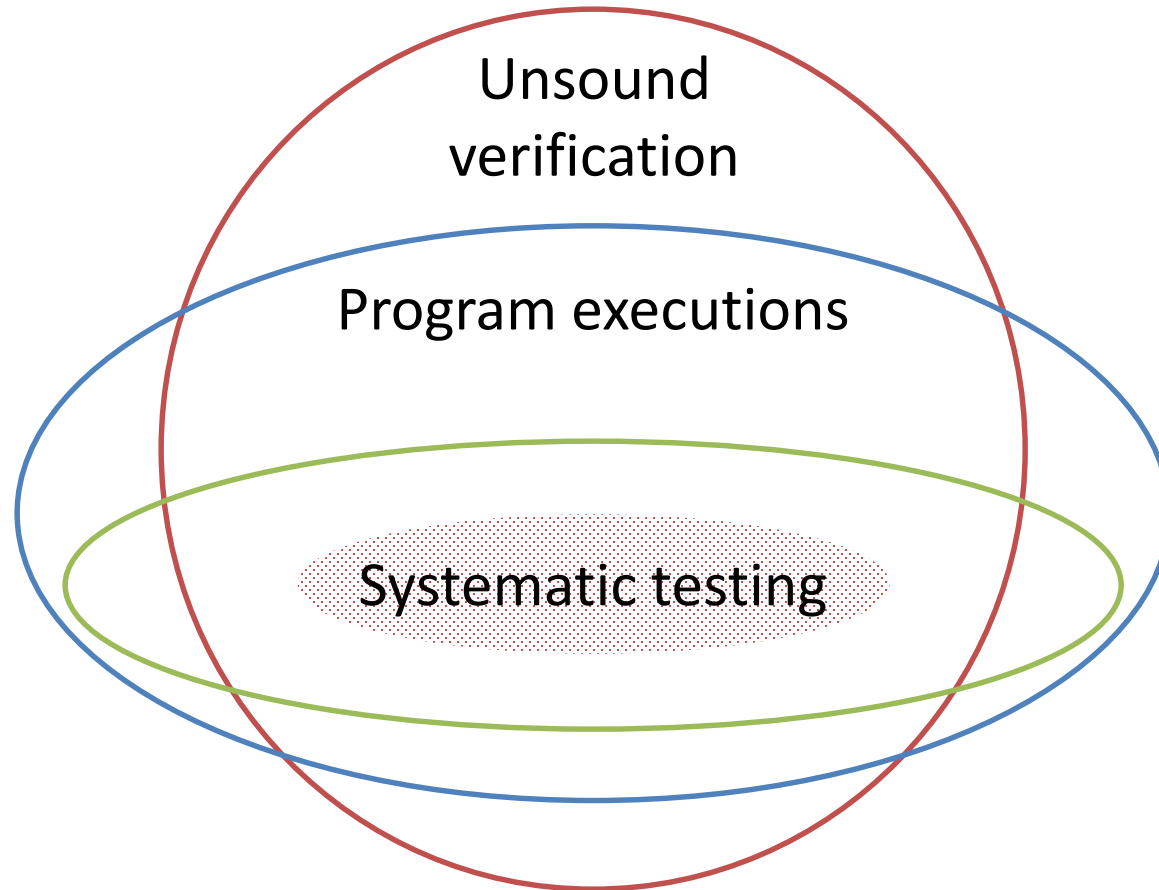
Verification and testing



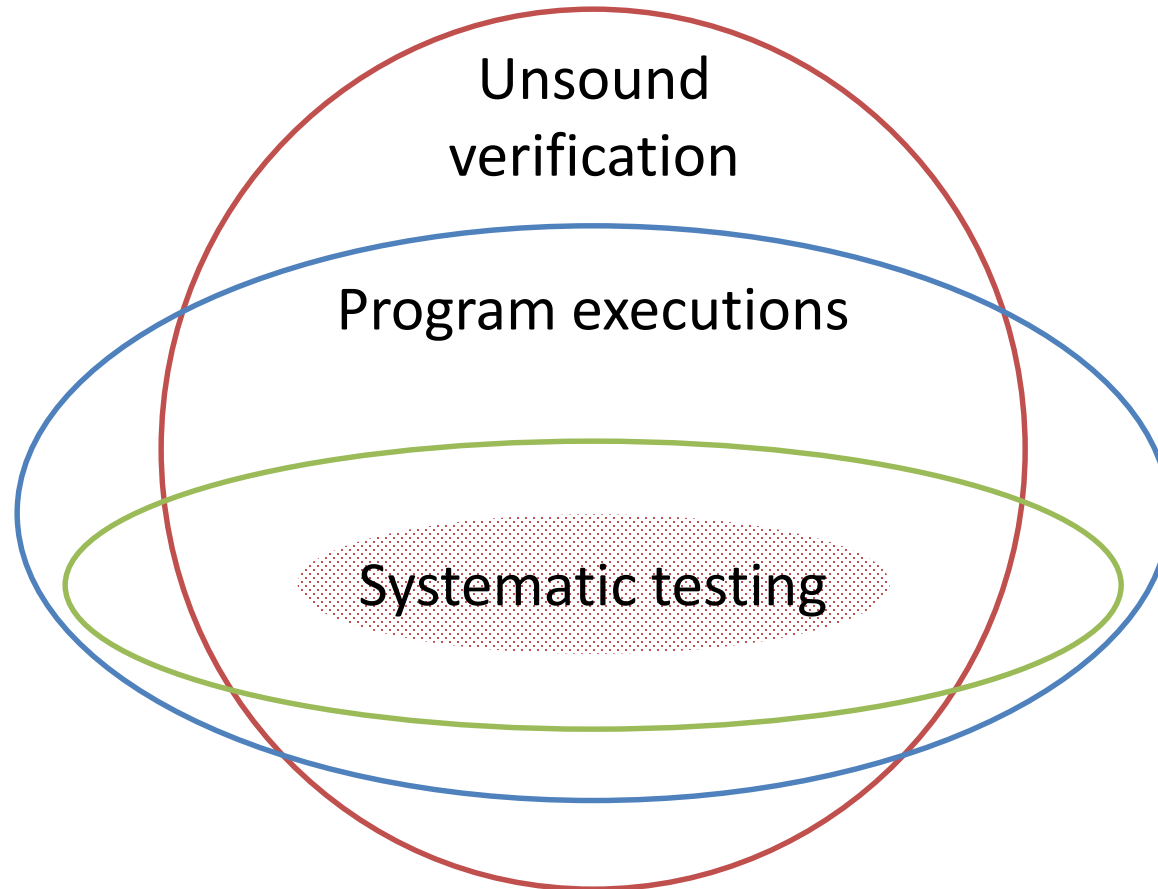
Verification and testing



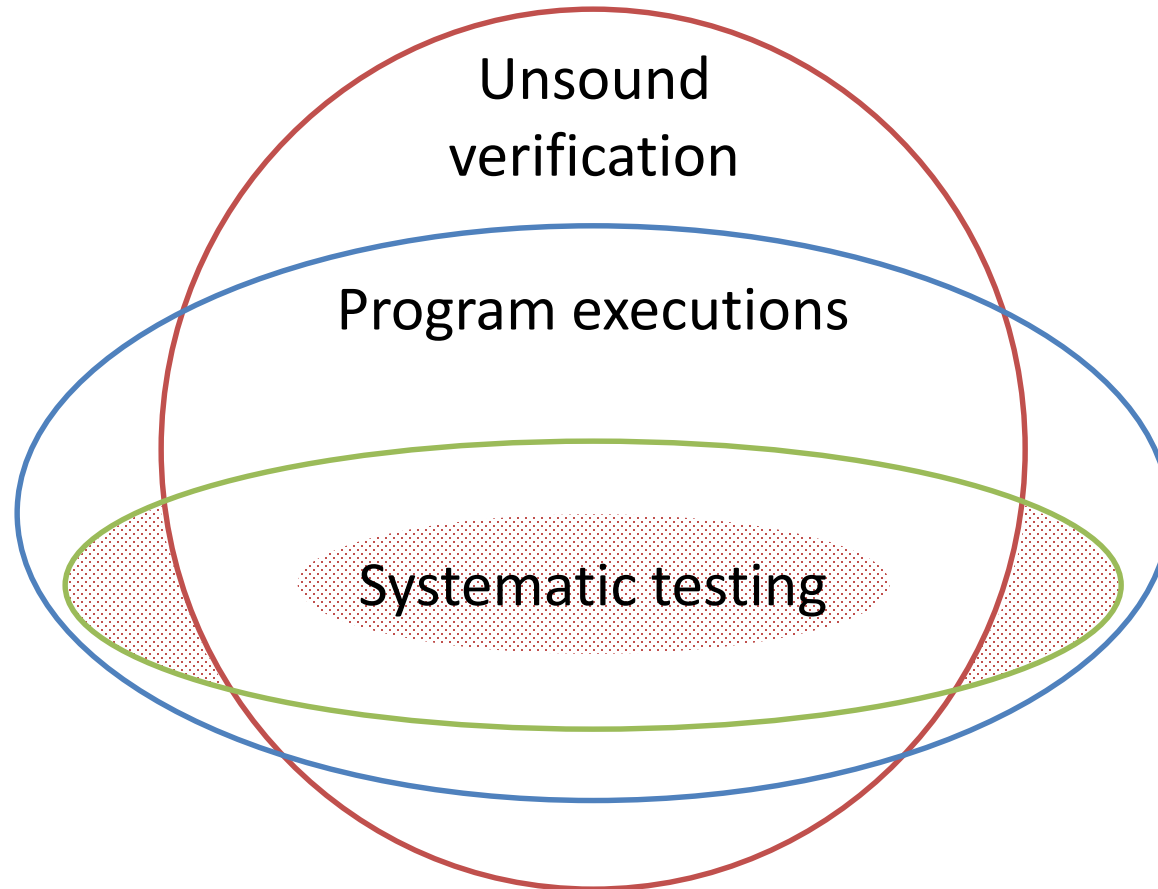
So far...



In our work...



In our work...



Static analysis

- Effective in detecting software errors
- Increasingly applied in industry
- Come in a wide range

Static analysis

- Effective in detecting software errors
- Increasingly applied in industry
- Come in a wide range

but...

Compromises

- Reduce the annotation overhead
- Reduce the number of false positives
- Increase performance
- Preserve modularity

Compromises

- Not checking program properties
- Making unjustified assumptions
- Being unsound

Example

```
void Deposit(int amount) { C#  
    if (amount <= 0 || amount > 50000) {  
        ReviewDeposit(amount);  
    } else {  
        balance = balance + amount;  
        if (balance > 10000) {  
            SuggestInvestment();  
        }  
    }  
    assert balance >= old(balance);  
}
```

Example

```
void Deposit(int amount) {  
    if (amount <= 0 || amount > 50000) {  
        ReviewDeposit(amount);  
    } else {  
        balance = balance + amount;  
        if (balance > 10000) {  
            SuggestInvestment();  
        }  
    }  
    assert balance >= old(balance);  
}
```



Example

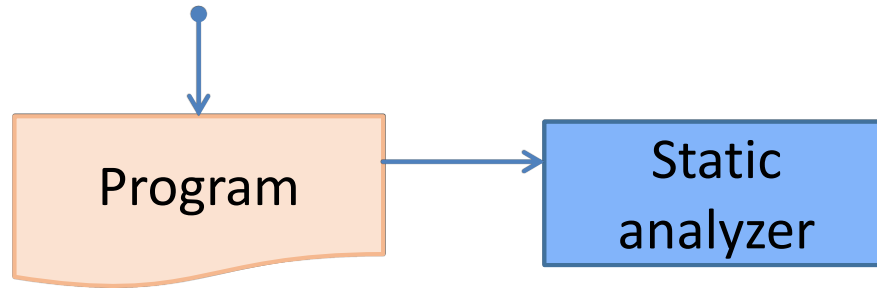
```
void Deposit(int amount) {  
    if (amount <= 0 || amount > 50000) {  
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    } else {  
        balance = balance + amount;  
        if (balance > 10000) {  
            SuggestInvestment();  
        }  
    }  
    assert balance >= old(balance);  
}
```



Consequences

- Absence of errors **not** guaranteed
- Test effort **not** reduced

Architecture

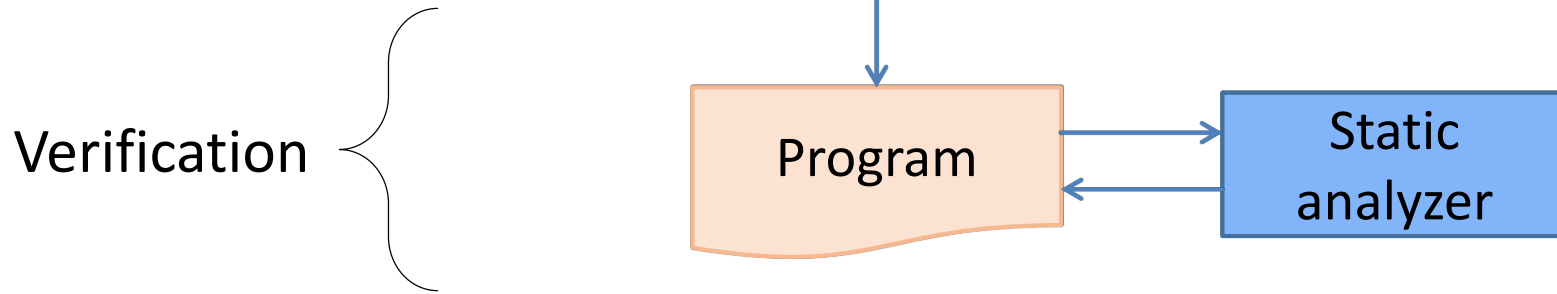


Annotations

```
void Deposit(int amount) {  
    if (amount <= 0 || amount > 50000) {  
        ReviewDeposit(amount);  
    } else {  
        assumed noOverflowAdd(balance, amount) as a;  
        balance = balance + amount;  
        if (balance > 10000) {  
            SuggestInvestment();  
        }  
    }  
    assert balance >= old(balance) verified a;  
}
```



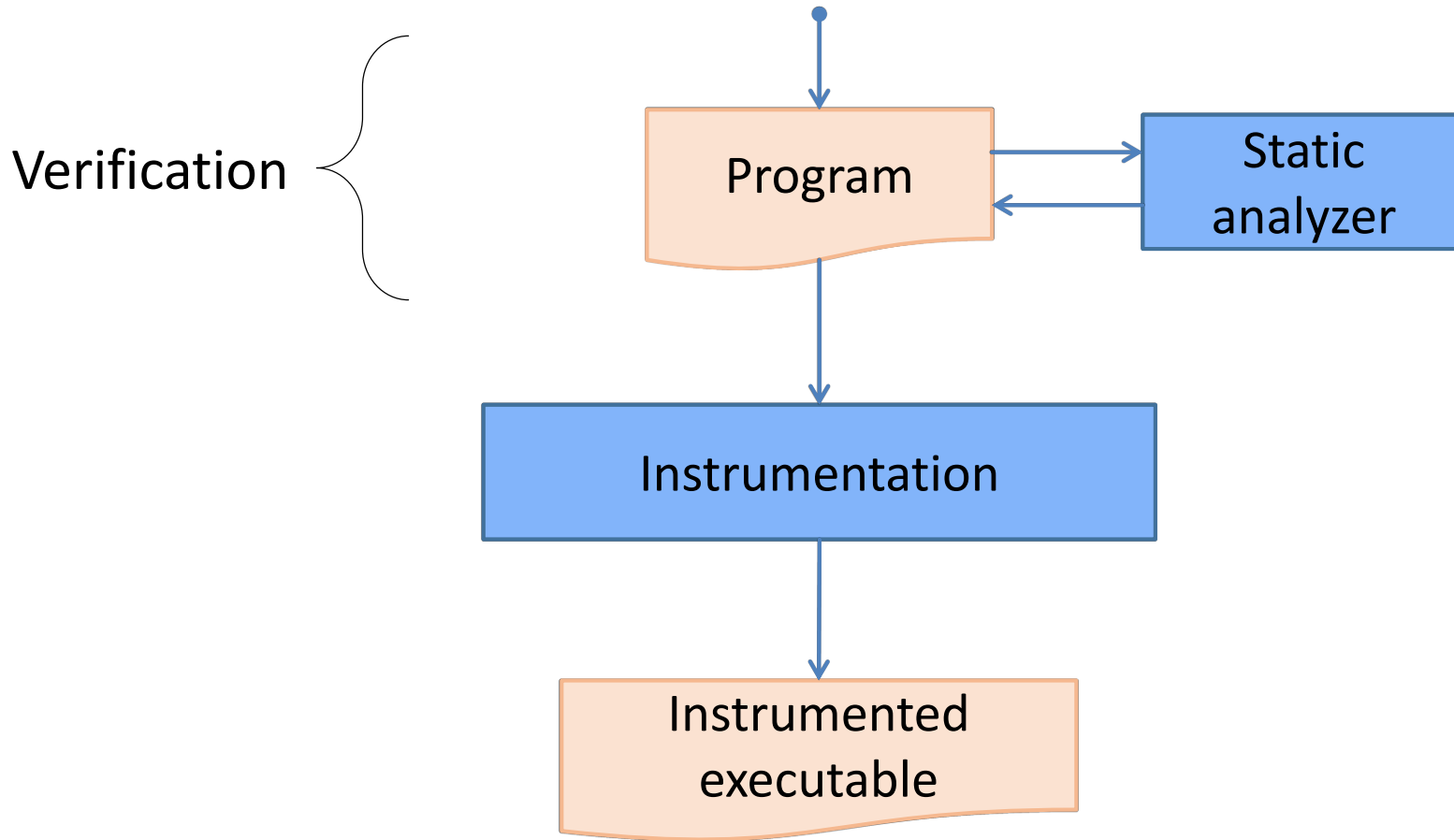
Architecture



Instrumentation

```
void Deposit(int amount) { Rewriter
    var a = true;
    if (amount <= 0 || amount > 50000) {
        ReviewDeposit(amount);
    } else {
        a = a && noOverflowAdd(balance, amount);
        balance = balance + amount;
        if (balance > 10000) {
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        }
    }
    assume a ==> balance >= old(balance);
    assert balance >= old(balance);
}
```

Architecture



Dynamic test generation

```
void Deposit(int amount) { Rewriter  
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    if (balance > 10000) {  
      SuggestInvestment();  
    }  
  }  
  assume a ==> balance >= old(balance);  
  assert balance >= old(balance);  
}
```


```
amount = 0  
balance = 0
```

Dynamic test generation

```
void Deposit(int amount) {
    var a = true;
    if (amount <= 0 || amount > 50000) {
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Rewriter

```
amount = 0
balance = 0
```



Dynamic test generation

```
void Deposit(int amount) { Rewriter  
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    }  
  }  
  assume a ==> balance >= old(balance);  
  assert balance >= old(balance);  
}
```


```
amount = 100  
balance = 0
```

Dynamic test generation

```
void Deposit(int amount) {
    var a = true;
    if (amount <= 0 || amount > 50000) {
        ReviewDeposit(amount);
    } else {
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Dynamic test generation

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    }  
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  assume a ==> balance >= old(balance);  
  assert balance >= old(balance);  
}
```


```
amount = 10001  
balance = 0
```

Dynamic test generation

```
void Deposit(int amount) {
    var a = true;
    if (amount <= 0 || amount > 50000) {
        ReviewDeposit(amount);
    } else {
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Rewriter

amount = 10001
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Dynamic test generation

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            SuggestInvestment();  
        }  
    }  
    assume a ==> balance >= old(balance);  
    assert balance >= old(balance);  
}
```


```
amount = 10001  
balance = int.MaxValue
```

Dynamic test generation

```
void Deposit(int amount) {
    var a = true;
    if (amount <= 0 || amount > 50000) {
        ReviewDeposit(amount);
    } else {
        a = a && noOverflowAdd(balance, amount);
        balance = balance + amount;
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    assume a ==> balance >= old(balance);
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Rewriter

```
amount = 10001
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```



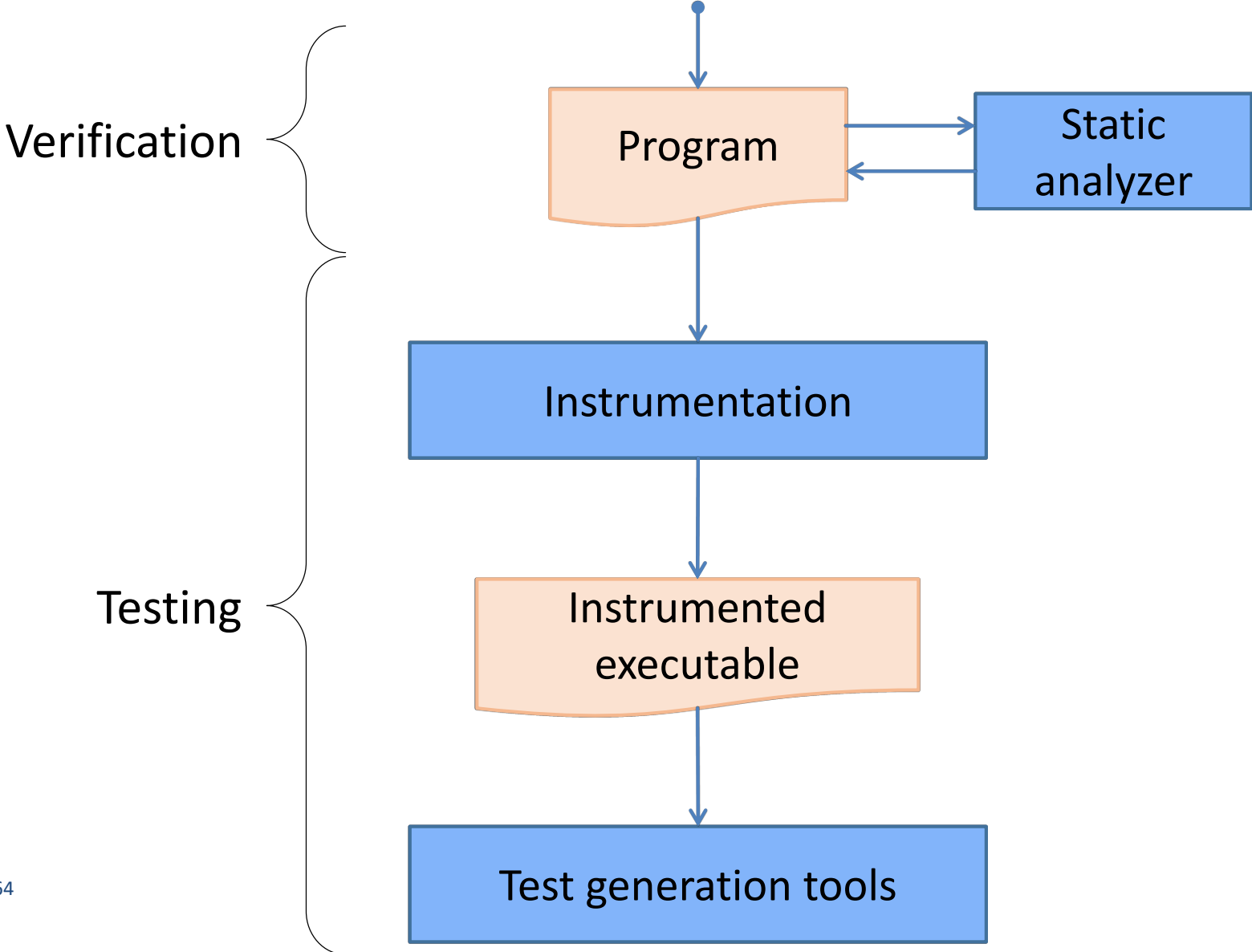
Dynamic test generation

```
void Deposit(int amount) {
    var a = true;
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    } else {
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    }
    assume a ==> balance >= old(balance);
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}
```

Rewriter

amount = ...
balance = ...

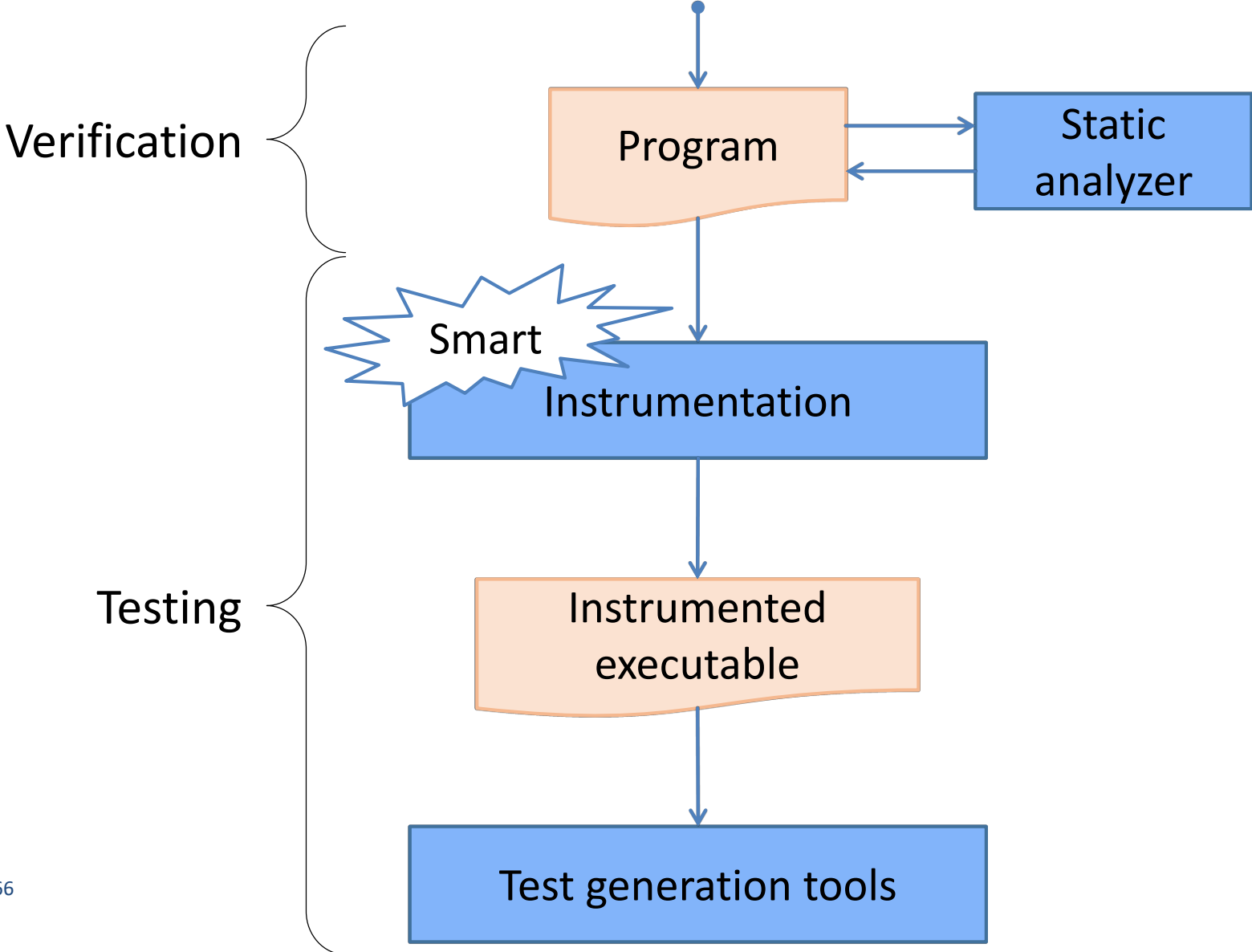
Architecture



Problem

```
void Deposit(int amount) { Rewriter
    var a = true;
    if (amount <= 0 || amount > 50000) {
        ReviewDeposit(amount);
    } else {
        a = a && noOverflowAdd(balance, amount);
        balance = balance + amount;
        if (balance > 10000) {
            SuggestInvestment();
        }
    }
    assume a ==> balance >= old(balance);
    assert balance >= old(balance);
}
```

Architecture



Smart instrumentation

Idea:

- Propagate conditions about **unverified executions** higher up in the control flow

Under the hood:

- Compute an abstraction of the program
- Infer conditions about unverified executions
- Instrument the concrete program

Abstraction

```
void Deposit(int amount) {  
  
    if (amount <= 0 || amount > 50000) {  
        ReviewDeposit(amount);  
    } else {  
        assumed noOverflowAdd(balance, amount) as a;  
        balance = balance + amount;  
        if (balance > 10000) {  
            SuggestInvestment();  
        }  
    }  
    assert balance >= old(balance) verified a;  
}
```



Abstraction

```
void Deposit(int amount) {  
    var a = true;  
    if (amount <= 0 || amount > 50000) {  
        ReviewDeposit(amount);  
    } else {  
        a = a && noOverflowAdd(balance, amount);  
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        if (balance > 10000) {  
            SuggestInvestment();  
        }  
    }  
    assert balance >= old(balance) verified a;  
}
```

Smart
rewriter

Abstraction

```
void Deposit {  
  var a = true;  
  if (*) {  
    call Account.ReviewDeposit;  
  } else {  
    a = a && *;  
  
    if (*) {  
      call Account.SuggestInvestment;  
    }  
  }  
  assert * verified a;  
}
```

Smart
rewriter

Abstraction

```
void Deposit {  
  var a = true;  
  if (*) {  
    call Account.ReviewDeposit;  
  } else {  
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    if (*) {  
      call Account.SuggestInvestment;  
    }  
  }  
  assert * verified a;  
}
```

Smart
rewriter

syntactic
non-deterministic
sound

Inference

```
void Deposit {  
    var a = true;  
    if (*) {  
        call Account.ReviewDeposit;  
    } else {  
        a = a && *;  
  
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Smart
rewriter

Inference

```
void Deposit {  
    var a = true;  
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    } else {  
        a = a && *;  
  
        if (*) {  
  
        }  
    }  
    assert * verified a;  
}
```

Smart
rewriter

Inference

```
void Deposit {  
  var a = true;  
  if (*) {  
  
  } else {  
    a = a && *;  
  
    if (*) {  
  
    }  
  }  
  assert * verified a; {false}  
}
```

Smart
rewriter

unverified executions
satisfy false

Inference

```
void Deposit {  
  var a = true;  
  if (*) {  
  
  } else {  
    a = a && *;  
  
    if (*) {  
  
    }  
  } {!a}  
  assert * verified a; {false}  
}
```

Smart
rewriter

unverified executions
satisfy !a

Inference

```
void Deposit {  
  var a = true;  
  if (*) {  
  
  } else { {true}  
    a = a && *;  
    {!a}  
    if (*) {  
      {!a}  
    } {!a}  
  } {!a}  
  assert * verified a; {false}  
}
```

Smart
rewriter

Inference

```
void Deposit {  
  var a = true;  
  if (*) {  
    {!a}  
  } else { {true}  
    a = a && *;  
    {!a}  
    if (*) {  
      {!a}  
    } {!a}  
  } {!a}  
  assert * verified a; {false}  
}
```

Smart
rewriter

Inference

```
void Deposit {  
  var a = true; {true}  
  if (*) {  
    {!a}  
  } else { {true}  
    a = a && *;  
    {!a}  
    if (*) {  
      {!a}  
    } {!a}  
  } {!a}  
  assert * verified a; {false}  
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Smart
rewriter

Inference

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void Deposit { {true}
  var a = true; {true}
  if (*) {
    {!a}
  } else { {true}
    a = a && *;
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    if (*) {
      {!a}
    } {!a}
  } {!a}
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Smart
rewriter

Inference

```
void Deposit { {true}
  var a = true; {true}
  if (*) {
    {!a}
  } else { {true}
    a = a && *;
    {!a}
    if (*) {
      {!a}
    } {!a}
  } {!a}
  assert * verified a; {false}
}
```

Smart
rewriter

$$wp(\text{assert } * \text{ verified } A, Q) \equiv A \wedge Q$$

Inference

```
void Deposit { {true}
  var a = true; {true}
  if (*) {
    {!a}
  } else { {true}
    a = a && *;
    {!a}
    if (*) {
      {!a}
    } {!a}
  } {!a}
  assert * verified a; {false}
}
```

Smart
rewriter

$$MAY(S) \equiv \neg wp(S, true)$$

Inference

```
void Deposit { {true}
  var a = true; {true}
  if (*) {
    {!a}
  } else { {true}
    a = a && *;
    {!a}
    if (*) {
      {!a}
    } {!a}
  } {!a}
  assert * verified a; {false}
}
```


Smart
rewriter

Smart instrumentation

```
void Deposit(int amount) {  
    var a = true;  
    if (amount <= 0 || amount > 50000) {  
        assume !a;  
        ReviewDeposit(amount);  
    } else {  
        a = a && noOverflowAdd(balance, amount);  
        assume !a;  
        balance = balance + amount;  
        if (balance > 10000) {  
            SuggestInvestment();  
        }  
    }  
    assume a ==> balance >= old(balance);  
    assert balance >= old(balance);  
}
```

Smart
rewriter


Dynamic test generation

```
void Deposit(int amount) {  
    var a = true;  
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        if (balance > 10000) {  
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    }  
    assume a ==> balance >= old(balance);  
    assert balance >= old(balance);  
}
```

Smart
rewriter

```
amount = 0  
balance = 0
```

Dynamic test generation

```
void Deposit(int amount) {  
    var a = true;  
    if (amount <= 0 || amount > 50000) {  
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            SuggestInvestment();  
        }  
    }  
    assume a ==> balance >= old(balance);  
    assert balance >= old(balance);  
}
```

Smart
rewriter

```
amount = 100  
balance = 0
```

Dynamic test generation

```
void Deposit(int amount) {  
    var a = true;  
    if (amount <= 0 || amount > 50000) {  
        assume !a;  
        ReviewDeposit(amount);  
    } else {  
        a = a && noOverflowAdd(balance, amount);  
        assume !a;  
        balance = balance + amount;  
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        }  
    }  
    assume a ==> balance >= old(balance);  
    assert balance >= old(balance);  
}
```

Smart
rewriter

```
amount = 10001  
balance = int.MaxValue
```



Dynamic test generation

```
void Deposit(int amount) {  
    var a = true;  
    if (amount <= 0 || amount > 50000) {  
        assume !a;  
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    } else {  
        a = a && noOverflowAdd(balance, amount);  
        assume !a;  
        balance = balance + amount;  
        if (balance > 10000) {  
            SuggestInvestment();  
        }  
    }  
    assume a ==> balance >= old(balance);  
    assert balance >= old(balance);  
}
```

Smart
rewriter

amount = 10001
balance = 0



Dynamic test generation

```
void Deposit(int amount) {  
    var a = true;  
    if (amount <= 0 || amount > 50000) {  
        assume !a;  
        ReviewDeposit(amount);  
    } else {  
        a = a && noOverflowAdd(balance, amount);  
        assume !a;  
        balance = balance + amount;  
        if (balance > 10000) {  
            SuggestInvestment();  
        }  
    }  
    assume a ==> balance >= old(balance);  
    assert balance >= old(balance);  
}
```

Smart
rewriter

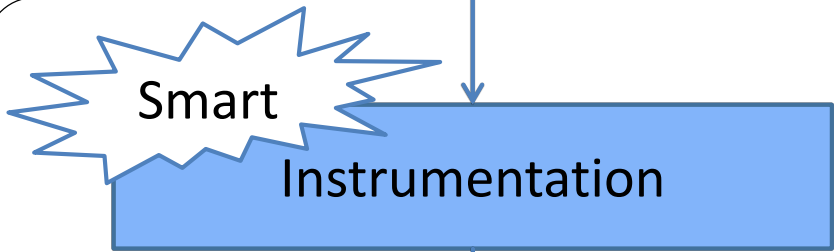
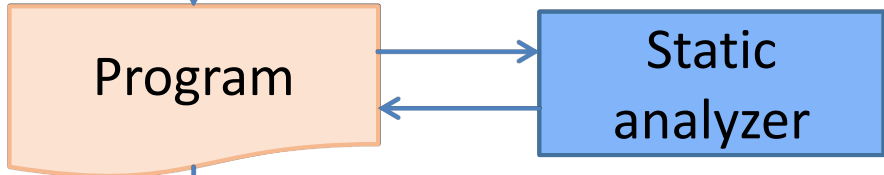
amount = ...
balance = ...



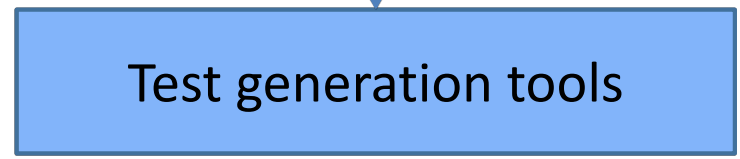
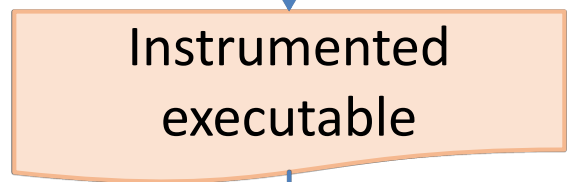
Architecture



Verification



Testing



Evaluation highlights

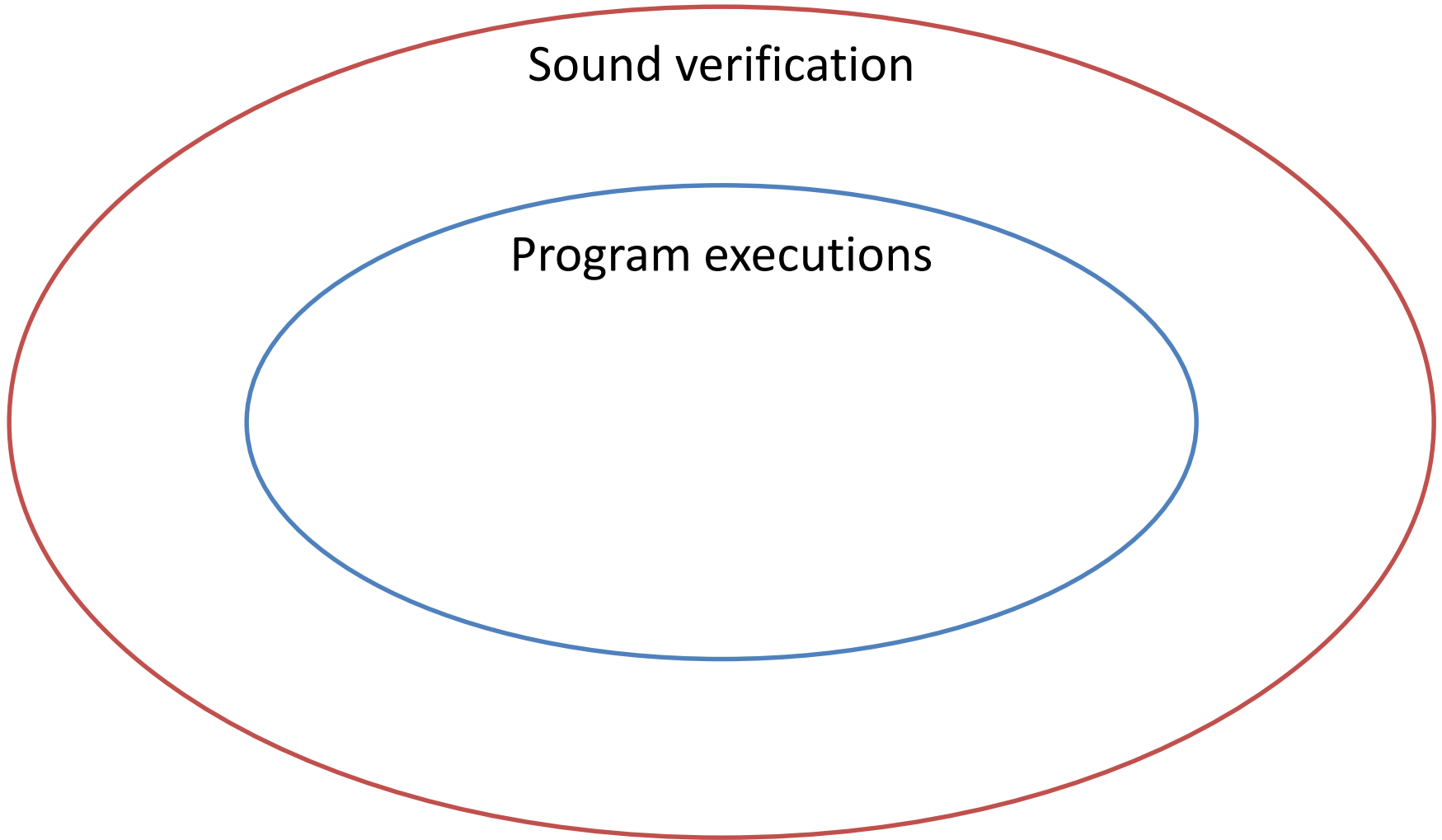
- 19.2% smaller test suites
- 7.1% more unverified executions
- 51.7% shorter testing time
- 29.3% fewer exploration bounds

Takeaways

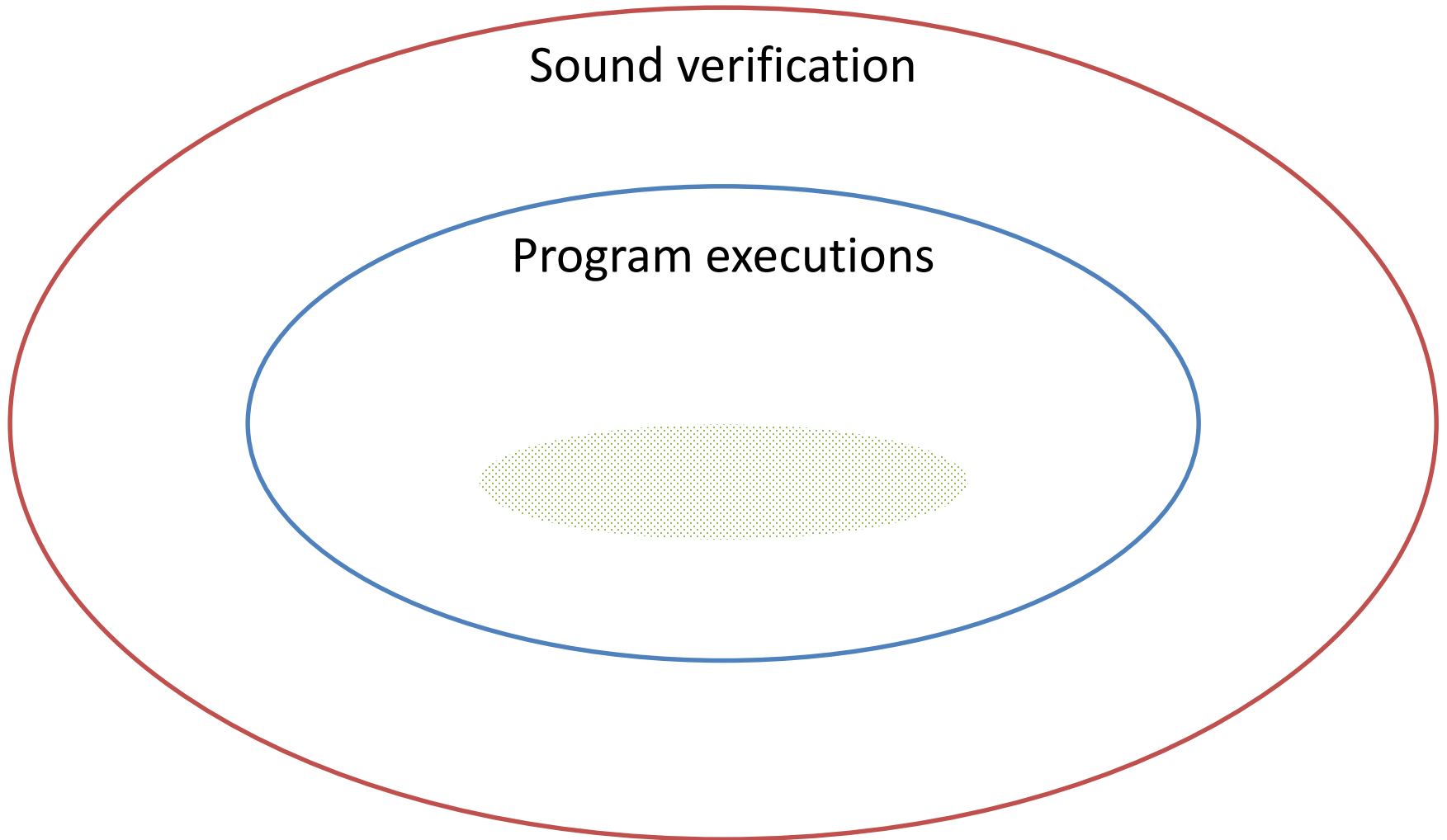
- Verification and systematic testing
 - Tight and effective collaboration
 - Increased software quality
 - Reduced test effort

Fun: Failure-Directed Program Trimming

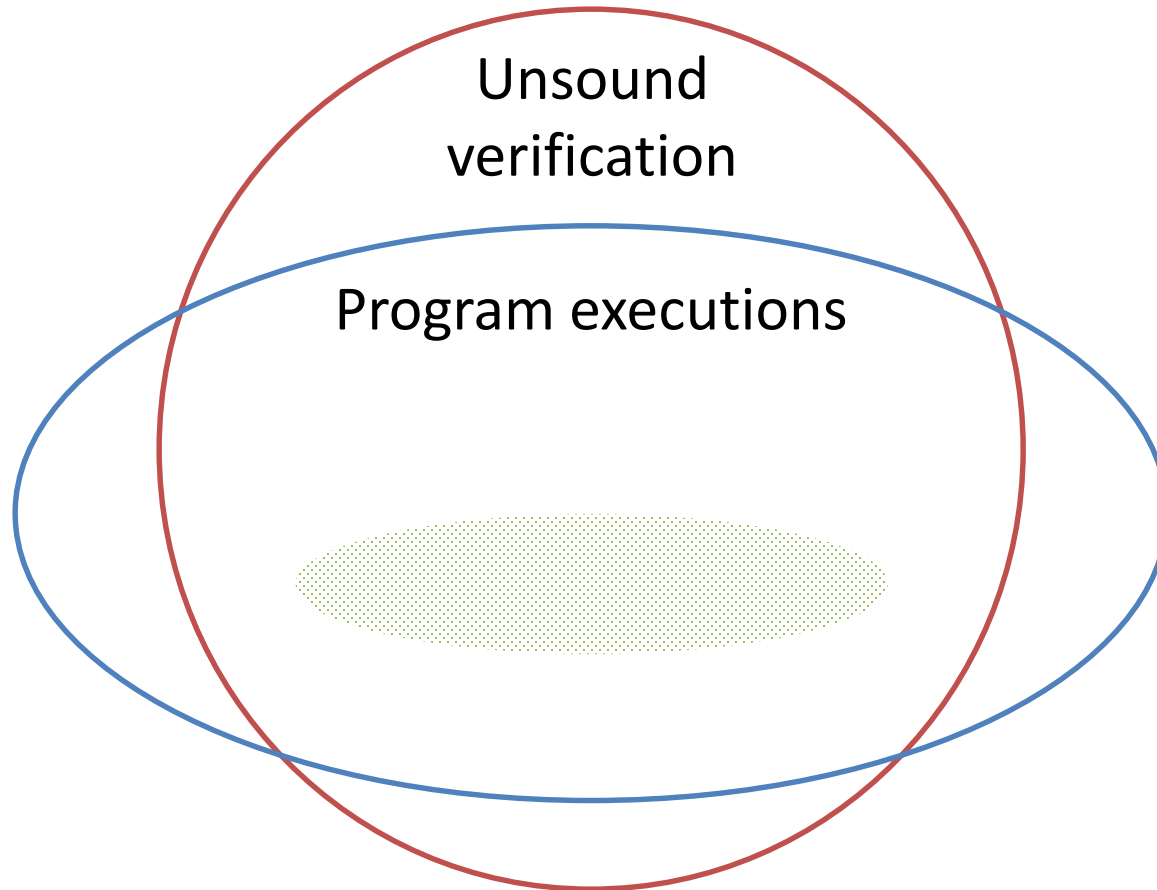
Safe executions



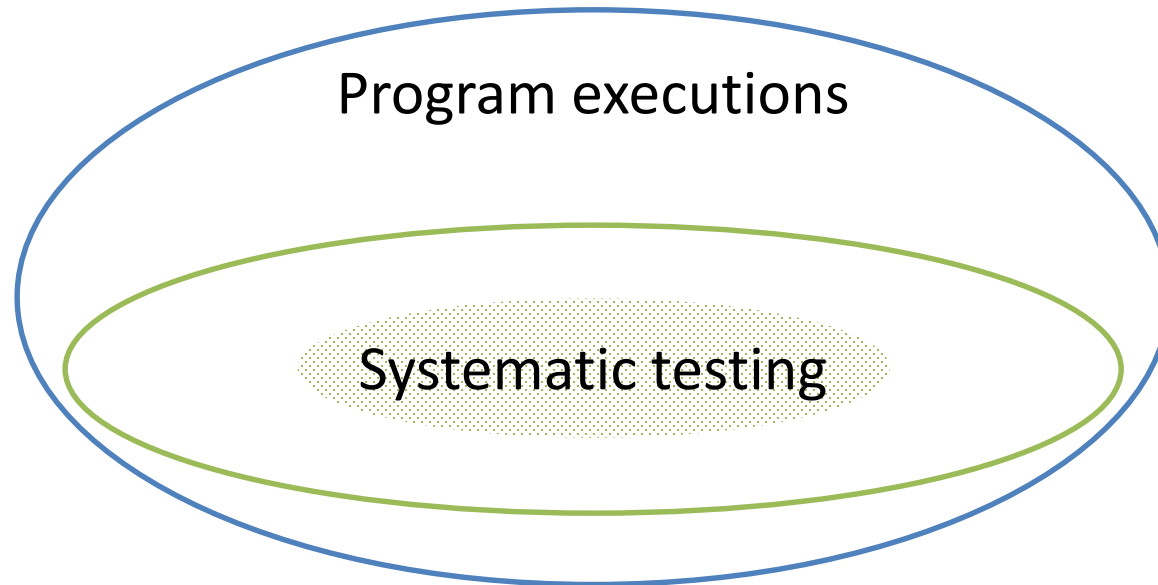
Safe executions



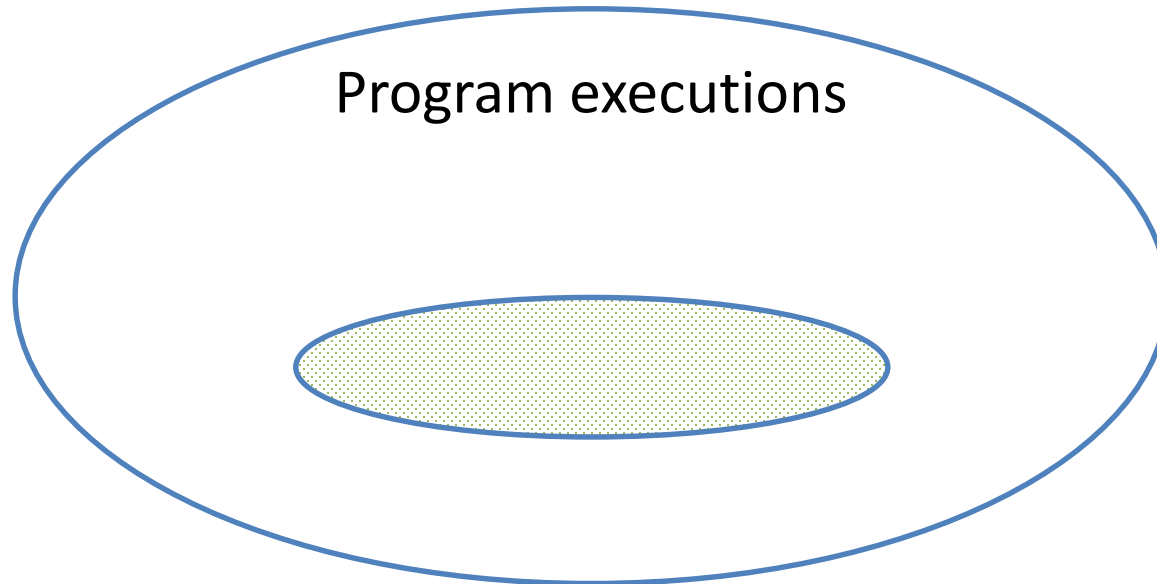
Safe executions



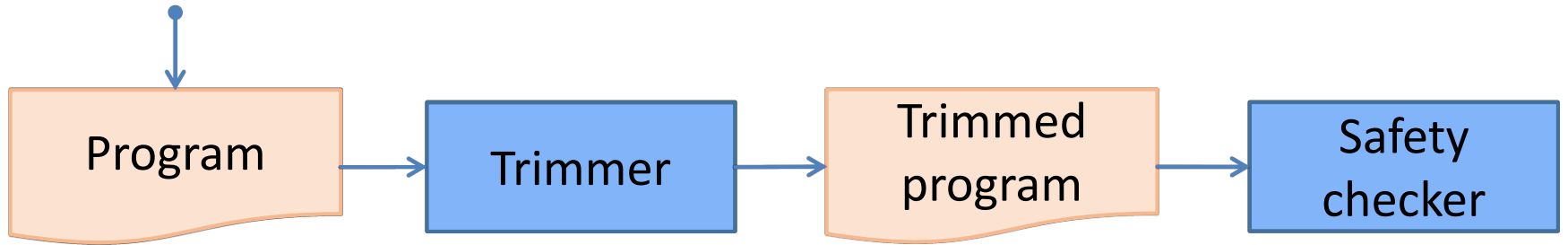
Safe executions



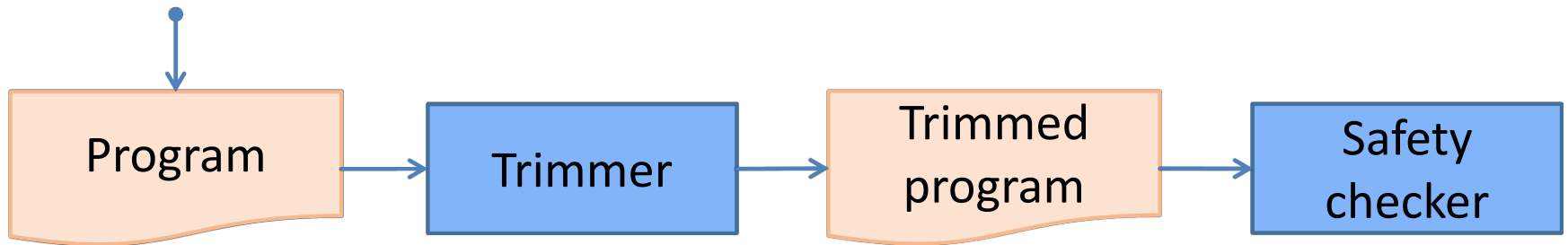
Trimming safe executions



Program trimming



Program trimming



- Simplifies programs
- Makes safety checkers **property directed**
- Improves **scalability** and **precision** of safety checkers

Example

```
x = *; y = *;      C

if (y > 0) {
  while (x < 10) {
    x = x + y;
  }
} else {
  x = x - 1;
}
assert x > 0;
```

Example

```
x = *; y = *;

if (y > 0) {
  while (x < 10) {
    x = x + y;
  }
} else {
  x = x - 1;
}
assert x > 0;
```

```
x = *; y = *;
assume y <= 0;
x = x - 1;
assert x > 0;
```

Trimmed program

- Given P , program trimming generates P_{tr}
- P and P_{tr} are equi-safe
- P_{tr} contains fewer execution paths than P

Example

```
x = *; y = *;  
  
if (y > 0) {  
    while (x < 10) {  
        x = x + y;  
    }  
} else {  
    x = x - 1;  
}  
assert x > 0;
```

```
x = *; y = *;  
assume y <= 0;  
x = x - 1;  
assert x > 0;
```

Example

```
x = *; y = *;      P

if (y > 0) {
  while (x < 10) {
    x = x + y;
  }
} else {
  x = x - 1;
}
assert x > 0;
```

```
x = *; y = *;      Ptr
assume y <= 0;
x = x - 1;
assert x > 0;
```


How to trim a program

- Statically infer **safety conditions**
- Negate the safety conditions to obtain **trimming conditions**
- **Instrument** the program with **assumptions** of the trimming conditions

Example

```
x = *; y = *;      P

if (y > 0) {
  while (x < 10) {
    x = x + y;
  }
} else {
  x = x - 1;
}
assert x > 0;
```

```
x = *; y = *;      Ptr
assume y <= 0;
x = x - 1;
assert x > 0;
```

Example

```
x = *; y = *;      P

if (y > 0) {
  while (x < 10) {
    x = x + y;
  }
} else {
  x = x - 1;
}
assert x > 0;
```

```
x = *; y = *;      Ptr
assume y <= 0;
if (y > 0) {
  while (x < 10) {
    x = x + y;
  }
} else {
  x = x - 1;
}
assert x > 0;
```

Condition properties

- Safety conditions are **sufficient for correctness**
- To be lightweight, we infer **stronger** safety conditions
- Trimming conditions are **necessary for failure**
- By definition, assuming the trimming conditions **preserves unsafe executions**

Benefit 1: Scalability

```
int fact(int n) {
    assume 0 <= n;
    int r = 1;
    if (n != 0) {
        r = n * fact(n - 1);
    }
    return r;
}

void main() {
    int m = *;

    int f = fact(m);
    assert m != 123 || f == 0;
}
```

Benefit 1: Scalability

```
int fact(int n) {  
    assume 0 <= n;  
    int r = 1;  
    if (n != 0) {  
        r = n * fact(n - 1);  
    }  
    return r;  
}  
  
void main() {  
    int m = *;  
  
    int f = fact(m);  
    assert m != 123 || f == 0;  
}
```



Benefit 1: Scalability

```
int fact(int n) {  
    assume 0 <= n;  
    int r = 1;  
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void main() {  
    int m = *;  
  
    int f = fact(m);  
    assert m != 123 || f == 0;  
}
```



Benefit 1: Scalability

```
int fact(int n) {  
    assume 0 <= n;  
    int r = 1;  
    if (n != 0) {  
        r = n * fact(n - 1);  
    }  
    return r;  
}
```

```
void main() {  
    int m = *;  
  
    int f = fact(m);  
    assert m != 123 || f == 0;  
}
```

$m \neq 123 \vee f = 0$

Benefit 1: Scalability

```
int fact(int n) {  
    assume 0 <= n;  
    int r = 1;  
    if (n != 0) {  
        r = n * fact(n - 1);  
    }  
    return r;  
}  
  
void main() {  
    int m = *;  
  
    int f = fact(m);  
    assert m != 123 || f == 0;  
}
```

m ≠ 123

Benefit 1: Scalability

```
int fact(int n) {
    assume 0 <= n;
    int r = 1;
    if (n != 0) {
        r = n * fact(n - 1);
    }
    return r;
}

void main() {
    int m = *;
    assume m == 123;
    int f = fact(m);
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Benefit 1: Scalability

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int fact(int n) {  
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```
void main() {  
    int m = *;  
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Benefit 1: Scalability

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int fact(int n) {  
    assume 0 <= n;  
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    if (n != 0) {  
        r = n * fact(n - 1);  
    }  
    return r;  
}
```



```
void main() {  
    int m = *;  
    assume m == 123;  
    int f = fact(m);  
    assert m != 123 || f == 0;  
}
```



Benefit 2: Precision

```
int fact(int n) {
    assume 0 <= n;

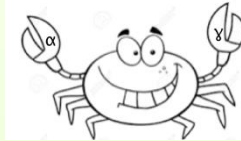
    int r = 1;
    if (n != 0) {
        r = n * fact(n - 1);
    }
    assert n != 0 || r == 1;
    return r;
}

void main() {
    int m = *;

    int f = fact(m);
}
```

Benefit 2: Precision

```
int fact(int n) {  
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    }  
    assert n != 0 || r == 1;  
    return r;  
}  
  
void main() {  
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    int f = fact(m);  
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```



Benefit 2: Precision

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int fact(int n) {  
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    if (n != 0) {  
        r = n * fact(n - 1);  
    }  
    assert n != 0 || r == 1;  
    return r;  
}  
  
void main() {  
    int m = *;  
  
    int f = fact(m);  
}
```

$n = 0$

Benefit 2: Precision

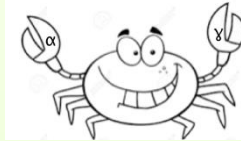
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Benefit 2: Precision

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    if (n != 0) {  
        r = n * fact(n - 1);  
    }  
    assert n != 0 || r == 1;  
    return r;  
}  
  
void main() {  
    int m = *;  
  
    int f = fact(m);  
}
```



Inference of safety conditions

- Lightweight, summary-based static analysis
- Similar to a weakest-precondition computation

Inference of safety conditions

- Lightweight, summary-based static analysis
- Similar to a weakest-precondition computation

but...

Inference of safety conditions

- Lightweight, summary-based static analysis
- Similar to a weakest-precondition computation

but...

- Relies on several inference innovations
 - Heap writes
 - Procedure calls

Evaluation highlights

- 26-60% more safe programs with three abstract domains of C_{RAB}
- The cheapest trimming configuration proves 23% more programs safe than the most expensive C_{RAB} configuration in less than half of the time

Evaluation highlights

- 16-18% more safe programs with three search strategies of K_{LEE}
- K_{LEE} with trimming explores 30-39% fewer paths
- The total running time of K_{LEE} decreases by 23-36%

Evaluation highlights

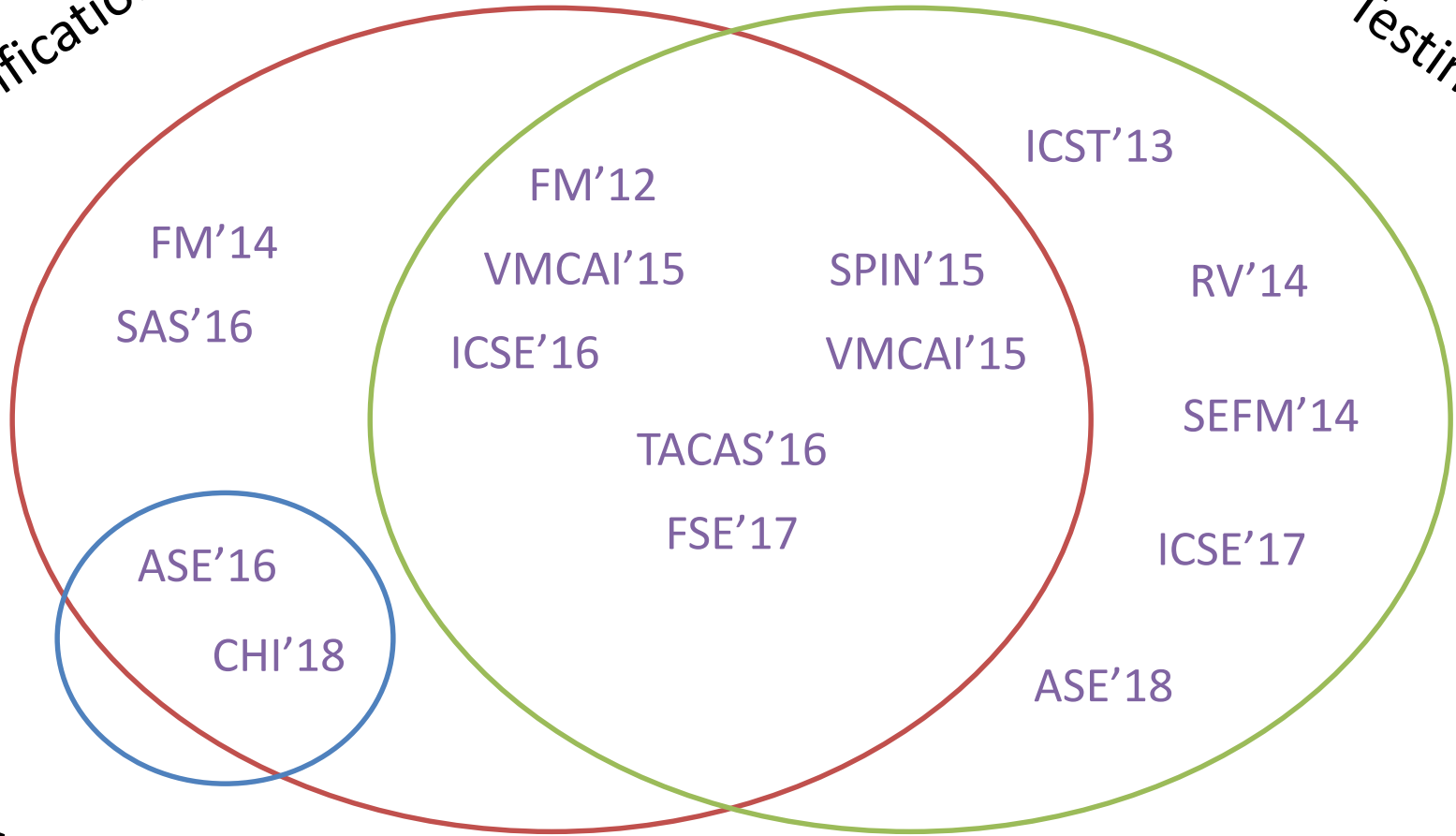
- The total time for trimming all benchmarks ranges from 5-9 secs

Takeaways

- Program trimming, a program simplification technique
 - Reduce the number of execution paths
 - Preserve unsafe executions of the original program
 - Positively impact efficiency and precision of safety checkers

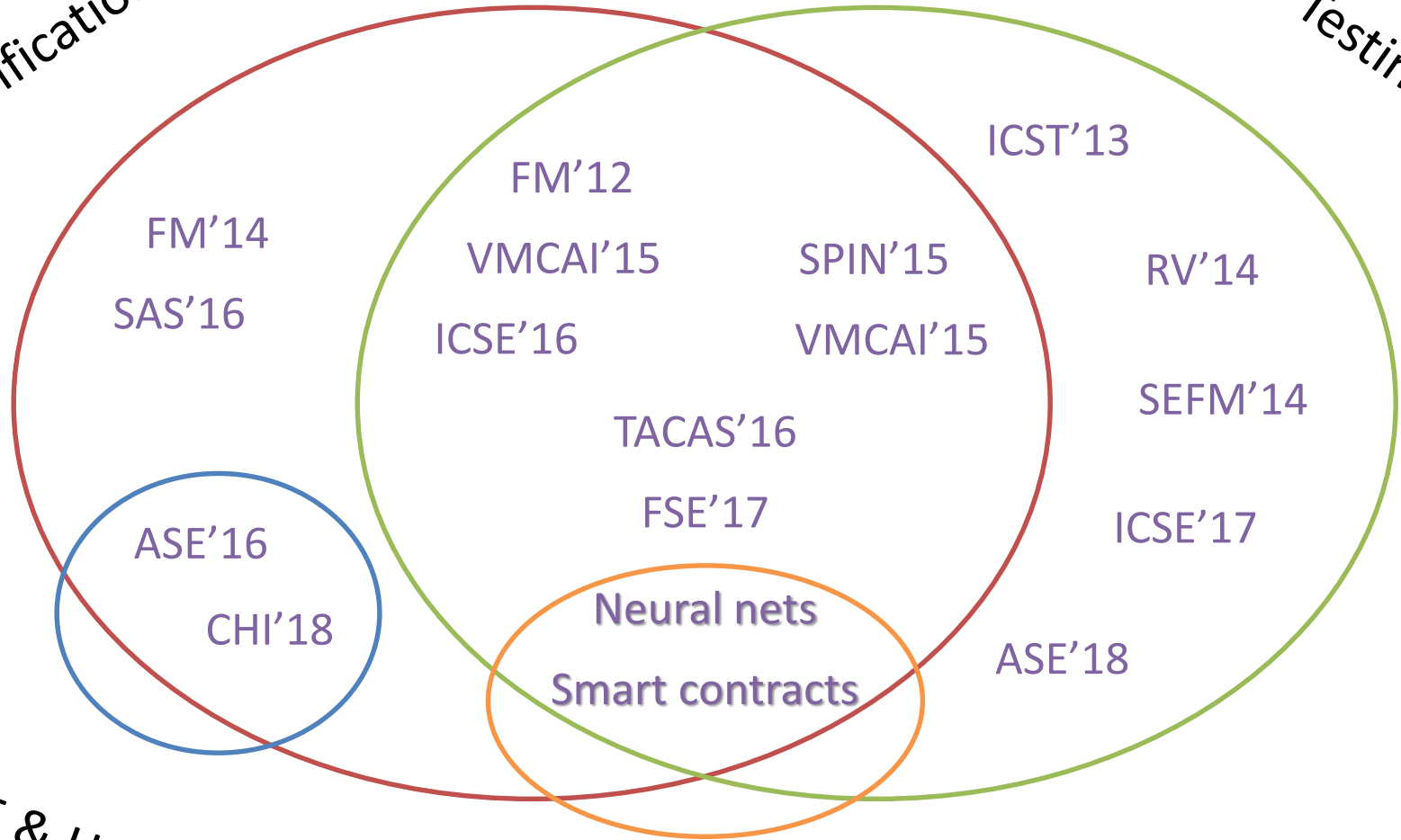
Verification

Testing



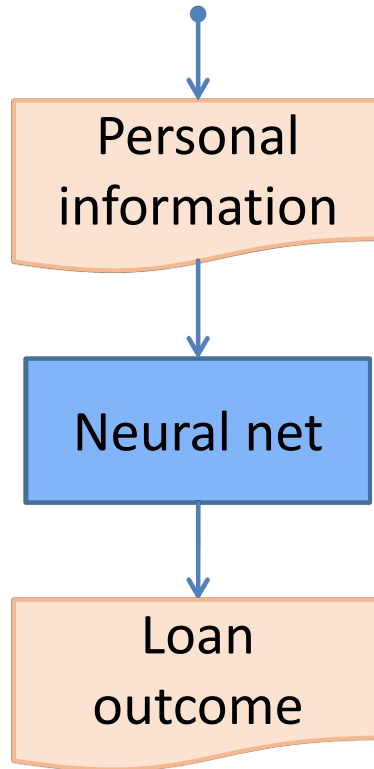
Verification

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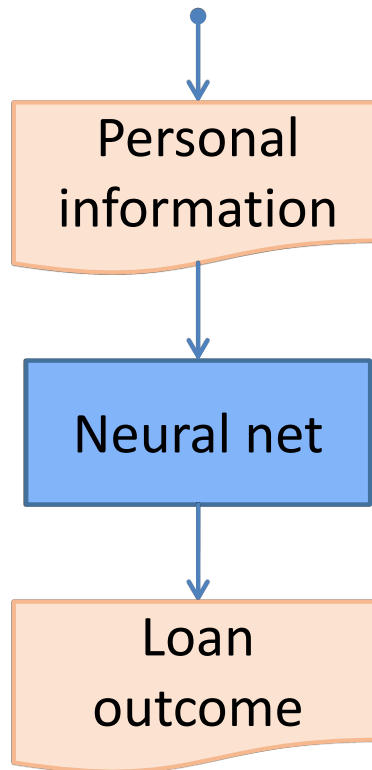


Security & Privacy

Neural nets



Neural nets



Which parts of the input affect which output?

Are there privacy concerns?

Smart contracts

- Manage digital assets according to a protocol
- May jeopardize significant amounts of money
- Have subtle interactions at execution time
- Are written in expressive languages

Smart contracts

- Manage digital assets according to a protocol
- May jeopardize significant amounts of money
- Have subtle interactions at execution time
- Are written in expressive languages

How to effectively detect security vulnerabilities?

How to help developers understand their possible behaviors?

Shameless plug

I am looking for motivated and talented students and interns!



Static Program Analysis Meets Test Case Generation

Maria Christakis
MPI-SWS, Germany